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S. No. of Question Paper : 88

Unique Paper Code : 32351101

I

Name of the Paper : Calculus

Name of the Course : B.Sc. (H) Mathematics

Semester : I

Duration : 3 Hours

Maximum Marks : 75

(Write your Roll No. on the top immediately on receipt of this question paper.)

All the sections are compulsory.

All questions carry equal marks.

Use of non-programmable scientific calculator is allowed.

Section I

(Attempt any four questions from Section I)

1. If $y = \log (x + \sqrt{x^2 + 1})$, show that :

$$(1 + x^2)y_{n+2} + (2n + 1)xy_{n+1} + n^2y_n = 0.$$

2. Sketch the graph of the function

$$f(x) = \frac{3x - 5}{x - 2}$$

by determining all critical points, intervals of increase and decrease, points of relative maxima and minima, concavity of the graph, inflection points and horizontal and vertical asymptotes.



3. Evaluate : $\lim_{x \rightarrow 0} (e^x - 1 - x)^x$.
4. Given the cost $C(x) = \frac{1}{8}x^2 + 5x + 98$ of producing x units of a particular commodity and the selling price $p(x) = \frac{1}{2}(75 - x)$ when x units are produced. Determine the level of production that maximizes profit.
5. Sketch the graph of $r = \sin 2\theta$ in polar coordinates.

Section II

(Attempt any *four* questions from Section II)

6. Obtain the reduction formula for

$$\int \sec^n x \, dx.$$

Use it to evaluate $\int \sec^6 x \, dx$.

7. Find the volume of the solid generated by revolving the region enclosed by $y = x$, $y = 2 - x^2$ and $x = 0$ is revolved about the x -axis.
8. Use cylindrical shells method to find the volume of the solid generated when the region enclosed by $y = 2x - x^2$ and $y = 0$ is resolved about y -axis.
9. Show that the arc length of the curve $y = \cosh x$ between $x = 0$ and $x = \log 2$ is $3/4$.
10. Find the area of the surface generated by revolving the curve $y = \sqrt{9 - x^2}$, $-1 \leq x \leq 1$, about x -axis.



Section III

(Attempt any *three* questions from Section III)

11. Find the equation of parabola having axis $y = 0$ and passing through the points $(3, 2)$ and $(2, -3)$.
12. Find the equation of ellipse with foci $(1, 2)$ and $(1, 4)$ and minor axis of length 2.
13. Describe and sketch the graph of the conic

$$x^2 - 4y^2 + 2x + 8y - 7 = 0.$$

Label the vertices, foci and asymptotes to the graph.

14. Rotate the coordinate axes to remove the xy -term in the equation

$$31x^2 + 10\sqrt{3}xy + 21y^2 - 144 = 0.$$

Identify the resultant conic.

Section IV

(Attempt any *four* questions from Section IV)

15. Given the vector functions

$$\vec{F}(t) = t\mathbf{i} + t^2\mathbf{j} + t^3\mathbf{k}$$

and

$$\vec{G}(t) = \frac{1}{t}\mathbf{i} - e^t\mathbf{j}$$

verify that

$$\lim_{t \rightarrow 1} [\vec{F}(t) \times \vec{G}(t)] = [\lim_{t \rightarrow 1} \vec{F}(t)] \times [\lim_{t \rightarrow 1} \vec{G}(t)].$$

P.T.O.



16. A velocity of particle moving in space is

$$\vec{V}(t) = t^2 \hat{i} - e^{2t} \hat{j} + \sqrt{t} \hat{k}.$$

Find the particle's position as a function of t if the position at time $t = 0$ is $\vec{R}(0) = \hat{i} + 4\hat{j} - \hat{k}$.

17. A shell is fired at ground level with a muzzle speed of 280 ft/s and at an elevation of 45° from ground level :

- (i) Find the maximum height attained by the shell.
- (ii) Find the time of flight and the range of the shell.

18. Find the tangential and normal components of the acceleration of an object that moves with position vector

$$\vec{R}(t) = \cos t \hat{i} + \sin t \hat{j} + t \hat{k}.$$

19. Find the curvature $\kappa(t)$ for the curve given by the vector equation

$$\vec{R}(t) = 4 \cos t \hat{i} + 4 \sin t \hat{j} + t \hat{k} \quad (0 \leq t \leq 2\pi).$$

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